

# Real-time implementation of the multi-swarm repetitive control algorithm

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## Outline

- 1 Repetitive control techniques
- 2 Plug-in direct particle swarm repetitive controller
- 3 Real-time implementation
- 4 Results and conclusion(s)



## Some known techniques and the novelty

- Multi-oscillatory (multi-resonant) controllers — the internal model principle (IEEE Trans. on Ind. Electron. 2015).



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- Repetitive neurocontrollers (the **derivative-based** approach) — a fairly new concept within the frame of 2D systems (IEEE IECON 2013).
- Direct particle swarm repetitive controller (the **derivative-free** approach) — a novelty within the frame of 2D systems (Archives of Electrical Engineering 4/2014).



## The motivation

The very basic P-type control law

$$u(p, k) = 1.0u(p, k - 1) + k_{RC}e(p, k - 1),$$

where  $u$  denotes the control signal,  $e$  is the control error,  $k_{RC}$  is the controller gain,  $k$  is the iteration (pass, trial, cycle) index and  $p$  is the time index along the pass ( $1 \leq p \leq \alpha$ , where  $\alpha$  is the pass length).

Theoretically perfect tracking could be achieved if only...

## The long-term stability issue

... this formula had been **stable**!

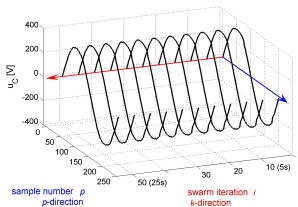
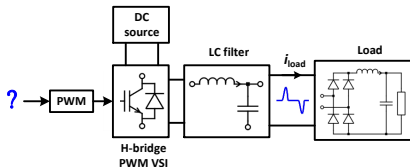
It then has to be modified into

$$u(p, k) = \cancel{1.0}^{\mathbf{Q}(z^{-1})} u(p, k-1) + \cancel{k_{RC}}^{\mathbf{L}(z^{-1})} e(p, k-1)$$

where **Q** and **L** are usually non-causal low-pass zero-phase-shift filters. This compromises the performance and hence **there still is plenty of room for new iterative learning techniques**.



## Two-dimensional (2D) behavior of a controller



### The objective

Rejection of a repetitive disturbance load current in a constant-amplitude constant-frequency VSI

## Let us attack the problem using DOP-capable PSO

- ✓ The repetitive control task at hand can be formulated as the DOP. It cannot be dealt with as the SOP because of a load current shape that can and will vary with time.
- ✓ Control tasks encountered in repetitive processes are ideally suited to be tackled with iterative DOP solvers – surprisingly, still not a widely recognized and acknowledged fact. Why?
- ✗ Online optimization techniques impose significant computational burden on a microcontroller.
- ✓ **PSO related calculations can be effectively distributed in time** and consequently implemented using an off-the-shelf industrial DSC – such as TI TMS320F2812.



# The control objective

## The cost function for the controller

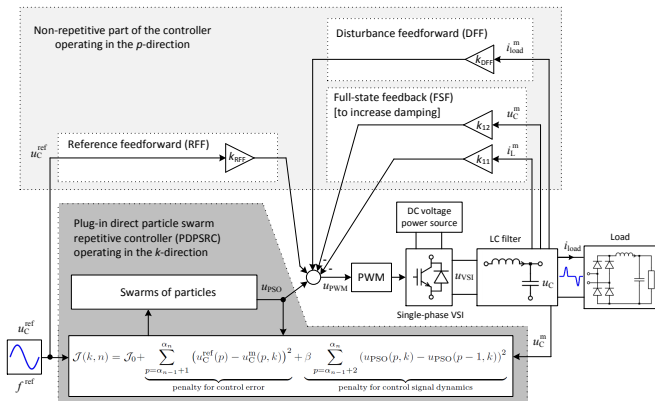
$$\begin{aligned}
 \mathcal{J}(k, n) = \mathcal{J}_0 + & \underbrace{\sum_{p=\alpha_{n-1}+1}^{\alpha_n} (u_C^{\text{ref}}(p) - u_C^m(p, k))^2}_{\text{penalty for control error}} + \\
 & + \beta \underbrace{\sum_{p=\alpha_{n-1}+2}^{\alpha_n} (u_{\text{PSO}}(p, k) - u_{\text{PSO}}(p-1, k))^2}_{\text{penalty for control signal dynamics}}
 \end{aligned}$$

## PSO algorithm

$$\mathbf{v}_{nj}(i+1)[p] = c_1 \mathbf{v}_{nj}(i) + c_2 r^{\text{pbest}}[p] \delta_p[p] \left( \mathbf{q}_{nj}^{\text{pbest}}[p] - \mathbf{q}_{nj}(i)[p] \right) + c_3 r^{\text{gbest}}[p] \delta_p[p] \left( \mathbf{q}_n^{\text{gbest}}[p] - \mathbf{q}_{nj}(i)[p] \right)$$

where:  $j$  is the particle identification number,  $n$  is the subswarm identification number and  $i$  denotes the swarm iteration number,  $\mathbf{v}_{nj}$  and  $\mathbf{q}_{nj}$  are speed and position of the  $j$ -th particle within the  $n$ -th subswarm,  $\mathbf{q}_{nj}^{\text{pbest}}$  stores the best solution proposed so far by the  $j$ -th particle ( $pbest$ ),  $\mathbf{q}_n^{\text{gbest}}$  denotes the best solution found so far by the swarm ( $gbest$ ),  $\delta_p$  is the attraction/repulsion variable for diversity control,  $r^{\text{pbest}}$  and  $r^{\text{gbest}}$  are random numbers uniformly distributed in the unit interval.

# Plug-in direct particle swarm repetitive ( $k$ -direction) controller with an accompanying non-repetitive ( $p$ -direction) controller

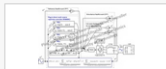


## [movie] Evolution of output voltage under variable load conditions

MATLAB CENTRAL

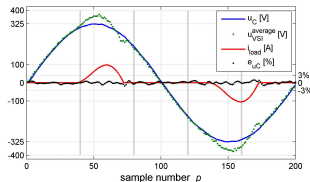
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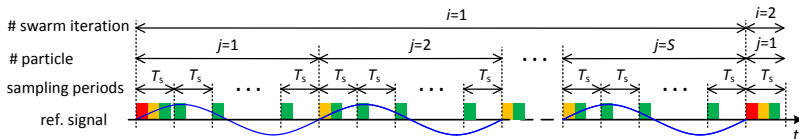
### Plug-in Direct Particle Swarm Repetitive Controller

by Bartłomiej Ufnalski  
14 Sep 2014 (Updated 15 Sep 2014)



Click on the pictures to play the movie.

## Time-distributed swarm calculations



## Hardware: TMS320F2812 eZdsp Starter Kit (socketed version)

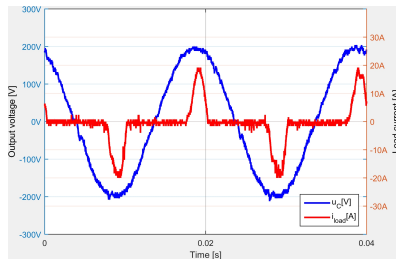
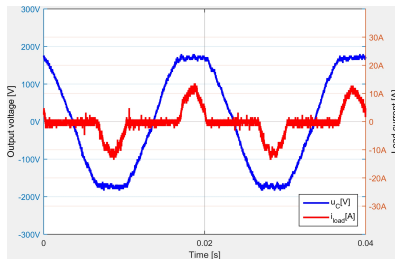


- ✓ 150 MHz clock speed available
- ✗ 18 K on chip RAM
- ✓ 128 K on chip FLASH ROM
- ✓ 64 K words on board RAM
- ✗ on board RAM access time

The first bottleneck (✗) is resolved by using an on-board (external) RAM.  
The second bottleneck (✗) is circumvented by rewriting variables from the on-board RAM to the on-chip RAM for their manipulation.



## Experimental verification





## Conclusions

- The novel swarm based repetitive control algorithm has been implemented in the off-the-shelf DSC @10kHz sampling time and @50Hz reference signal (200 samples per pass).



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- It has been demonstrated that the PSO technique can be used in online (real-time) mode to directly shape the control signal for the repetitive process.



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- The novel swarm based repetitive control algorithm has been implemented in the off-the-shelf DSC @10kHz sampling time and @50Hz reference signal (200 samples per pass).
- It has been demonstrated that the PSO technique can be used in online (real-time) mode to directly shape the control signal for the repetitive process.
- It is then feasible to interpret repetitive control tasks as dynamic optimization problems and solve them in real time using the particle swarm optimization technique – the technique almost exclusively associated in power electronics (up to now) with static offline optimization problems.



## Questions?

# Thank you for your kind attention!

And please do not hesitate to contact us at

✉ [\*\*bartlomiej.ufnalski@ee.pw.edu.pl\*\*](mailto:bartlomiej.ufnalski@ee.pw.edu.pl) .

This presentation is already available at

🌐 [\*\*www.ufnalski.edu.pl\*\*](http://www.ufnalski.edu.pl)

along with the relevant models/codes published at

🌐 [\*\*www.mathworks.com/matlabcentral/profile/authors/2128309-bartlomiej-ufnalski\*\*](http://www.mathworks.com/matlabcentral/profile/authors/2128309-bartlomiej-ufnalski) .

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